

Name _____

Objective: SWBAT Find the x or y value when the slope is given.

Warm up: Find the slope of the line that passes through the points.

1. $(-2, -1)$ and $(4, 5)$
 $x_1 \ y_1 \quad x_2 \ y_2$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{5 - (-1)}{4 - (-2)} = \frac{5 + 1}{4 + 2} = \frac{6}{6} = \boxed{1}$$

EXAMPLE 1: Find the value of x so that the line that passes through the points

$(2, 3)$ and $(x, 9)$ has a slope of $\frac{2}{3} = m$
 $x_1 \ y_1 \quad x_2 \ y_2$

Let $(x_1, y_1) = (2, 3)$ and $(x_2, y_2) = (x, 9)$

Write the formula for slope:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

And substitute

$$\frac{2}{3} = \frac{9 - 3}{x - 2} \text{ (cross product)} \quad \frac{2}{3} = \frac{6}{x - 2}$$

Then solve for x.

$$\begin{aligned} 3(6) &= 2(x - 2) \\ 18 &= 2x - 4 \\ +4 & \quad +4 \\ \hline 22 &= 2x \\ \frac{22}{2} &= \frac{2x}{2} \\ \boxed{11} &= x \end{aligned}$$

Example:

$$(5, 4) \text{ and } (-5, y); m = \frac{3}{5}$$

x_1, y_1 x_2, y_2

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{3}{5} = \frac{y - 4}{-5 - 5}$$

$$5(y - 4) = 3(-10)$$

$$\frac{3}{5} \frac{y - 4}{-10} \Rightarrow \frac{5y - 20 = -30}{+20 \quad +20}$$
$$\frac{5y = -10}{5 \quad 5}$$
$$\boxed{y = -2}$$

Now you try.....

$$(x, 4) \text{ and } (6, -1); m = \frac{5}{6}$$

x_1, y_1 x_2, y_2

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{5}{6} = \frac{-1 - 4}{6 - x} \Rightarrow \frac{5}{6} = \frac{-5}{6 - x}$$

$$5(6 - x) = -5(6)$$
$$\frac{30 - 5x = -30}{-30 \quad -30}$$
$$\frac{-5x = -60}{-5 \quad -5}$$
$$\boxed{x = 12}$$

More Examples:



$$(9, 3) \text{ and } (-6, 7y); m = 3$$

$x_1 \ y_1 \quad x_2 \ y_2$

$$(0, y) \text{ and } (-2, 1); m = -8$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{3}{1} = \frac{7y - 3}{-6 - 9} \quad (-6 + -9)$$

$$\frac{3}{1} = \frac{7y - 3}{-15}$$

$$3(-15) = 1(7y - 3)$$

$$\begin{array}{r} -45 = 7y - 3 \\ +3 \quad \quad +3 \end{array}$$

$$\frac{-42}{7} = \frac{7y}{7}$$

$$-6 = y$$